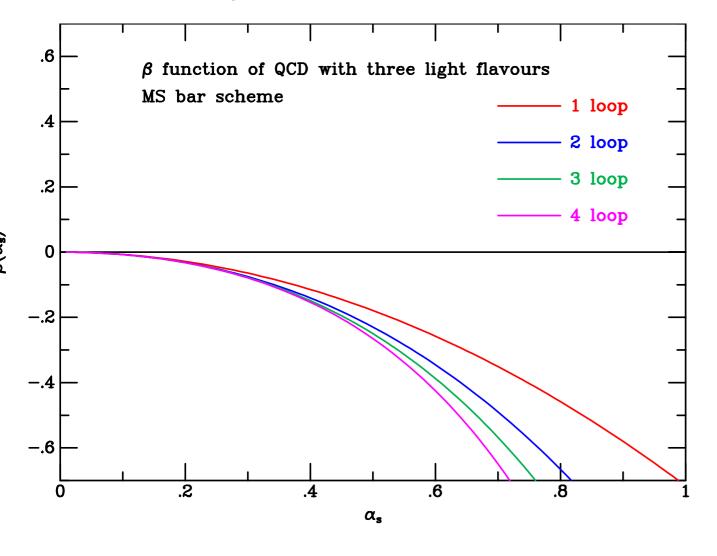
QCD in the 21st century

Keith Ellis Fermilab

Asymptotic freedom

Back in 1973....

$$\mu^2 \frac{\partial \alpha_S}{\partial \mu^2} = \beta(\alpha_S)$$





NAL-PUB-73/49-THY

July, 1973

Theory

ASYMPTOTICALLY FREE GAUGE THEORIES - I

David J. Gross

National Accelerator Laboratory

and

Joseph Henry Laboratories

Princeton University

Princeton, New Jersey 08540

and

Frank Wilczek

Joseph Henry Laboratories

Princeton University

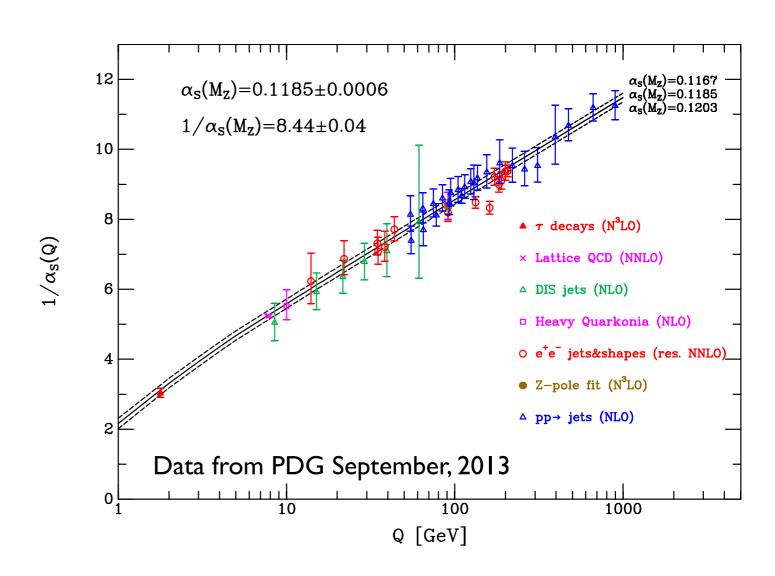
Princeton, New Jersey 08540

Research supported in part by the United States Air Force Office of Scientific Research under Contract F-44620-71-6-0180

[†]Alfred P. Sloan Foundation Research Fellow

Running coupling, α_s

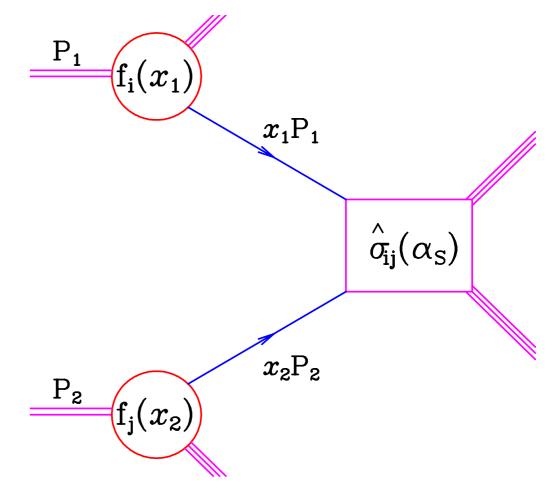
- Incontrovertible fact that α_s is smallish at energies accessible with current machines.
- $1/\alpha_s$ as grows as $\log (Q)$.
- $I/\alpha_s(Mz)=8.44$
- c.f QED: $1/\alpha(Mz)=128...$
- Radiative corrections ~15 times more important in QCD than QED.

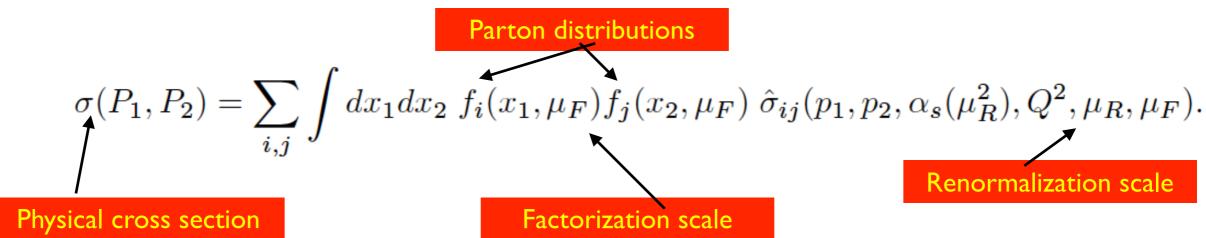


Also some other outliers mainly from e+e- data Abbate, 1006.3080, $\alpha_s(M_Z)$ =0.1135+0.0010 Hoang, 1501.04753, $\alpha_s(M_Z)$ =0.1123+0.0002

QCD improved parton model

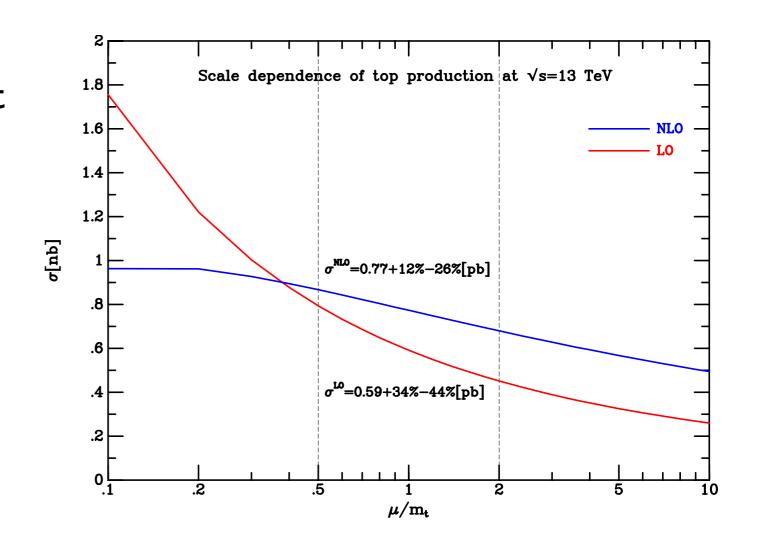
- Hard cross section is represented as a convolution of a short-distance cross section and non-perturbative parton distribution functions.
- Physical cross section is formally independent of μ_R and μ_F through the order calculated.
- Here we shall be concerned with the short distance cross section.





Higher order perturbative QCD: why bother?

- Take top pair production at 13 TeV.
- Higher order terms are not the 12% suggested by the size of α_s, because of the special nature of renormalization group improved perturbation theory.
- Given that e.g. the luminosity measurement at the LHC is in the range 2-5% we need to do better than 12% anyway.



$$\mu_R = \mu_F = \mu$$

Ingredients in a NLO calculation

Consider vector boson production

- Real and virtual diagrams live in different phase spaces
- For the virtual diagrams (lower multiplicity) the infrared poles are explicit, whereas as for real diagrams (higher multiplicity), they appear after integration.
- The necessity to integrate to cancel poles, is at variance with the desire for a differential distribution.

Perturbative QCD 2000-2010

- Prehistory
- MCFM (inclusion of many processes at NLO).
- NLO is the first approximation which gives an idea of a suitable choice for μ .
- The rise of automatic procedures.
- Semi-numerical methods for Feynman diagrams.
- Next-to-leading order (NLO) revolution

α_s corrections to the Drell-Yan process

- the birth of precision hadronic collider physics
- resolved ambiguities associated with the colour degree of freedom.
- The first 'K' factor calculation
- No agreement with data without NLO contributions.
- State of the art until NNLO was calculated NPB382 (1992) 11

LARGE PERTURBATIVE CORRECTIONS TO THE DRELL-YAN PROCESS IN QCD *

G. ALTARELLI

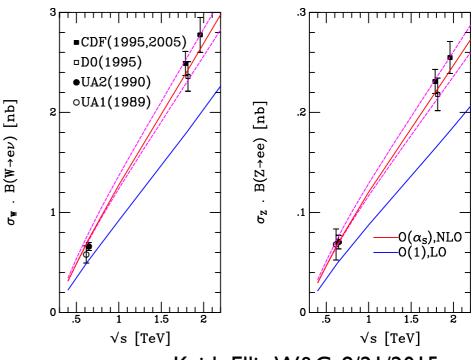
Istituto di Fisica dell' Università, Istituto Nazionale di Fisica Nucleare, Sezione di Roma, Rome 00185, Italy

R.K. ELLIS

Center for Theoretical Physics, Laboratory for Nuclear Science and Department of Physics, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139, USA

G. MARTINELLI Istituto Nazionale di Fisi Laboratori Nazionali di I Frascati 00044. Italy

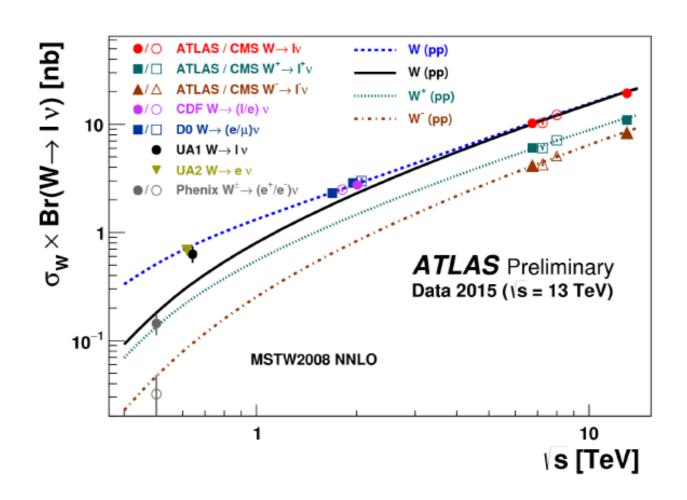




Keith Ellis, W&C, 8/21/2015

Comparison with data from low to high energy

- Basic DY
 mechanism is the
 same for W,Z
 production.
- Beautifully confirmed by W[±] production from $\sqrt{s}=0.54-13$ TeV.



But we need to go beyond total cross sections.....

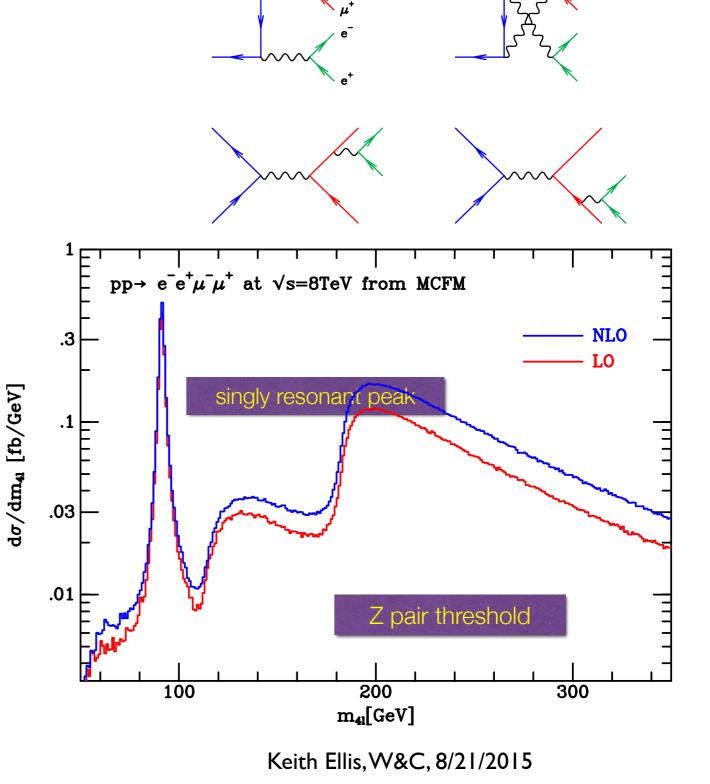
MCFM (Monte Carlo for FeMtobarn processes)



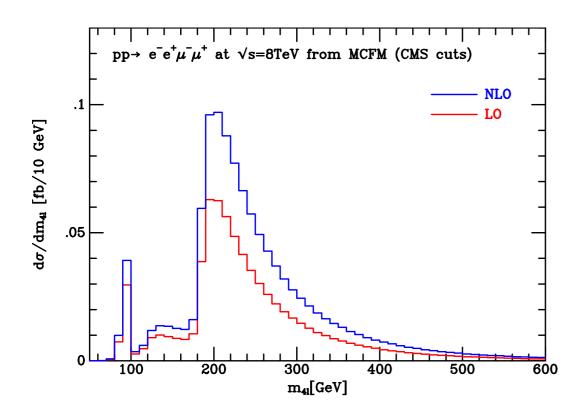
- MCFM is a parton-level Monte Carlo program that computes hadron-collider cross sections at NLO [Campbell, RKE, Williams]
- Gives access to explicit final states, distributions.
- Implements analytic results for matrix elements, so fast and numerically stable.
- Flexible, freely distributed code, widely used in the community
- Theoretical predictions for more than 300 processes, (extensive use at Tevatron and LHC, (cited by > 650 experimental papers).
- Significant role as a catalyst for other theoretical efforts.
- Eight updates to the code in the last eight years.

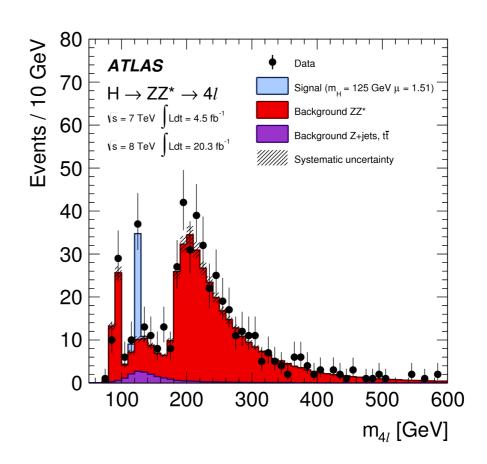
Vector boson pair production

- For the final states that we are interested in, we go beyond the doubly resonant approximation.
- Z-peak coming from singly resonant diagrams, important check of resolution in search for Higgs boson.
- NLO includes gg->ZZ, (but no Higgs yet, see later).

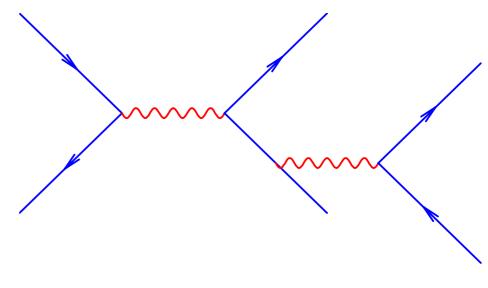


Singly resonant contribution and Higgs discovery



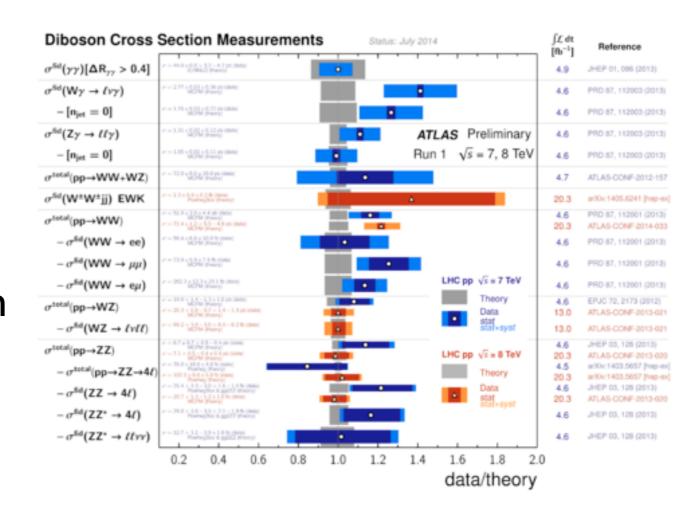


 Relative size of peaks depends sensitively on the cuts



Vector boson pair production

- Growth of Boson pair cross section with energy is an important check of gauge structure.
- For W+W-, no discrepancy in fiducial cross section.
- Emphasizes the importance of going beyond total rates.



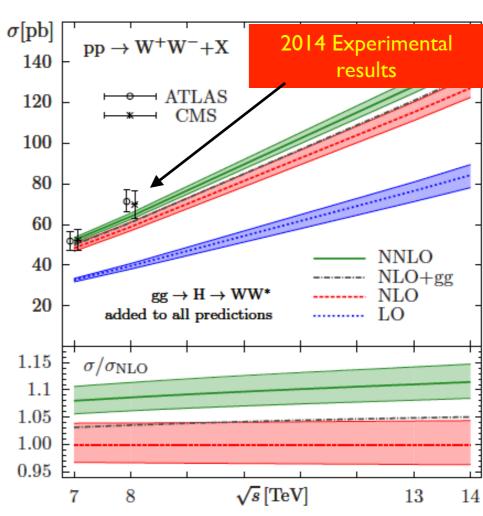
ATLAS results

	ATLAS @ 8 TeV	$\parallel pp \rightarrow l^+ l^- \nu \bar{\nu}$	$pp \rightarrow H \rightarrow l^+ l^- \nu \bar{\nu}$	total
$\begin{array}{c c} e^{+}\mu^{-} + e^{-}\mu^{+} \\ e^{+}e^{-} \\ \mu^{+}\mu^{-} \end{array}$	$ \begin{vmatrix} 377.8_{-6.8}^{+6.9}(\text{stat.})_{-22.2}^{+25.1}(\text{syst.})_{-10.7}^{+11.4}(\text{lumi.}) \\ 68.5_{-4.1}^{+4.2}(\text{stat.})_{-6.6}^{+7.7}(\text{syst.})_{-2.0}^{+2.1}(\text{lumi.}) \\ 74.4_{-3.2}^{+3.3}(\text{stat.})_{-6.0}^{+7.0}(\text{syst.})_{-2.1}^{+2.3}(\text{lumi.}) \end{vmatrix} $	$\begin{vmatrix} 332.4_{-2.3}^{+4.7} \\ 63.7_{-0.4}^{+0.8} \\ 69.3_{-0.4}^{+0.9} \end{vmatrix}$	$\begin{array}{c} 9.8^{+0.0}_{-1.2} \\ 2.2^{+0.0}_{-0.2} \\ 2.4^{+0.0}_{-0.2} \end{array}$	$\begin{array}{c} 342.2^{+4.7}_{-2.6} \\ 65.9^{+0.8}_{-0.4} \\ 71.7^{+0.9}_{-0.5} \end{array}$

Monni, Zanderighi 1410.4745

Necessity of NNLO

Gehrmann et al, 1408.5243



Einsweiler, Lepton Photon 2015

Di-boson production: W⁺W⁻ Production (CMS)

- Measure $\sigma(fid) = 60.1 \pm 0.9$ (stat) ± 3.2 (exp) ± 3.1 (theo) ± 1.6 (lumi) pb
- Theory σ(NNLO) = 59.8 ± 1.2 pb
- Good agreement (expt ± 8%), but NNLO calculations are really necessary.

Heavy quark production

- Improvement of perturbative stability as we proceed to NLO.
- Results apply to top, bottom, and perhaps charm production.
- State of the art until
 Czakon et al. 1303.6254

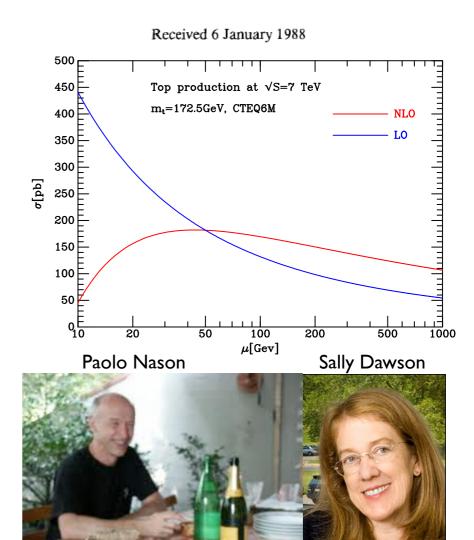
THE TOTAL CROSS SECTION FOR THE PRODUCTION OF HEAVY QUARKS IN HADRONIC COLLISIONS

P. NASON and S. DAWSON

Brookhaven National Laboratory, Upton, LI, NY 11973, USA

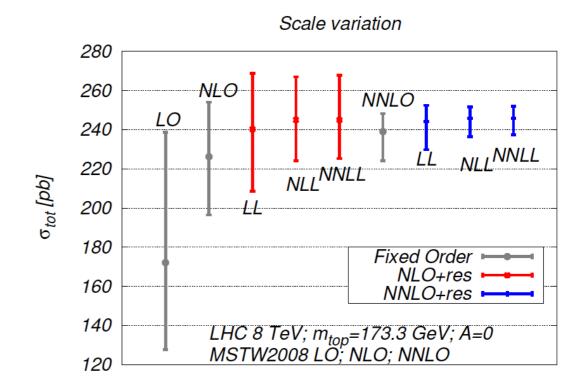
R.K. ELLIS

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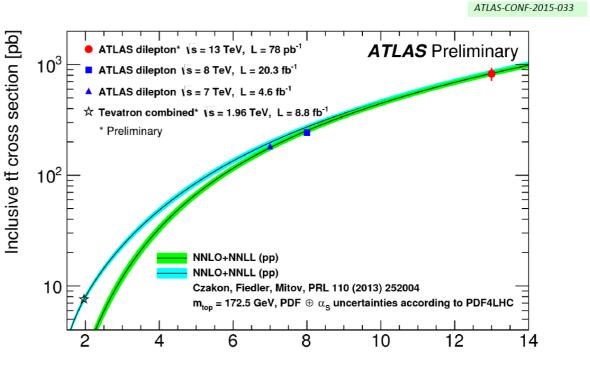


Rates for top production

- Progression of results as higher order terms were included.
- Emphasizes the importance of a true (N)NLO calculation.
- NNLO results beautifully confirmed by results at 7 and 13 TeV.



Czakon et al, 1305.3892

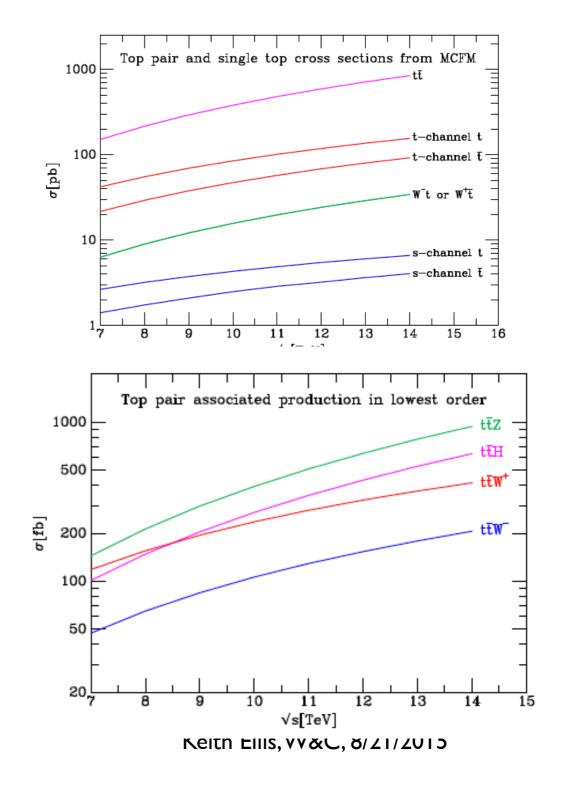


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Top, from signal to calibration to background.

- Top production grows rapidly with energy.
- Plethora of top-related processes.
 Top pair, single top, ttV, tV
 (V=electroweak boson), Top pair
 + 1,2,3,4, jets....
- We need to find a framework to include these processes, which is simpler than calculating the full final state.

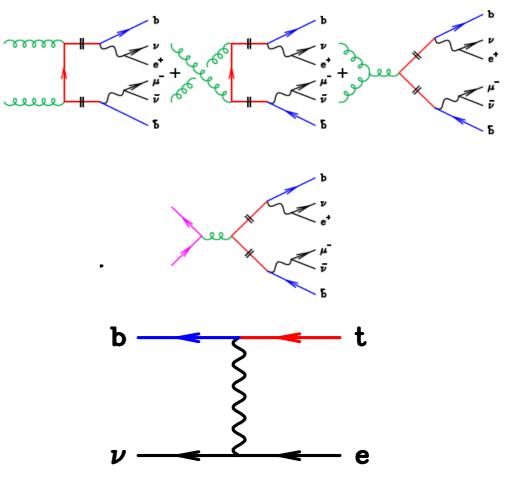
$$pp \to W^+W^-b\bar{b} \to \nu_e e^+\mu^-\bar{\nu}_\mu b\bar{b}$$



Practical proposal for top-related processes

Campbell, RKE 1204.1503

- Treat top quark as being on their mass-shells, but keep all spin correlations.
- For most variables the onshell approximation will be smeared by the finite energy resolution of the detector.
- Since the coupling to the W is left-handed, it is actually easier to keep spin correlations, than to drop them.

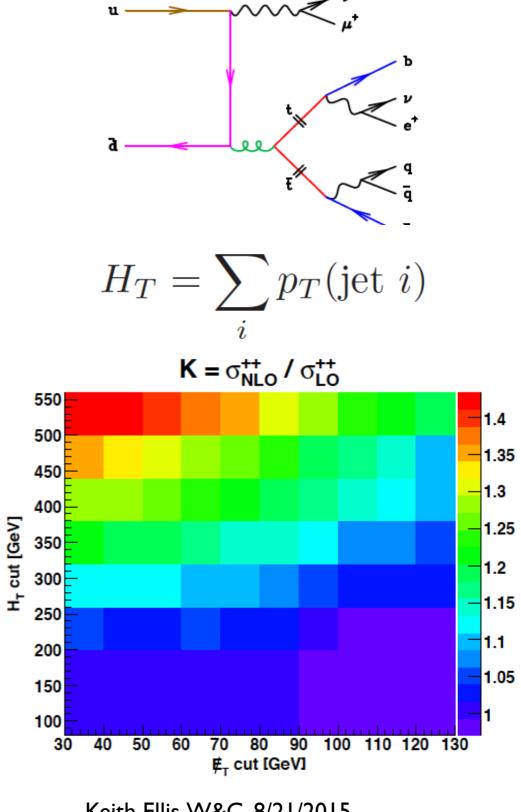


$$\langle \nu | \gamma^{\mu} \gamma_L | e] \times \bar{u}(b) \gamma_{\mu} \gamma_L (t + m_t) \dots$$

$$= 2 \bar{u}(b) | \nu \rangle \times [e | (t + m_t) \dots$$

Example: ttW

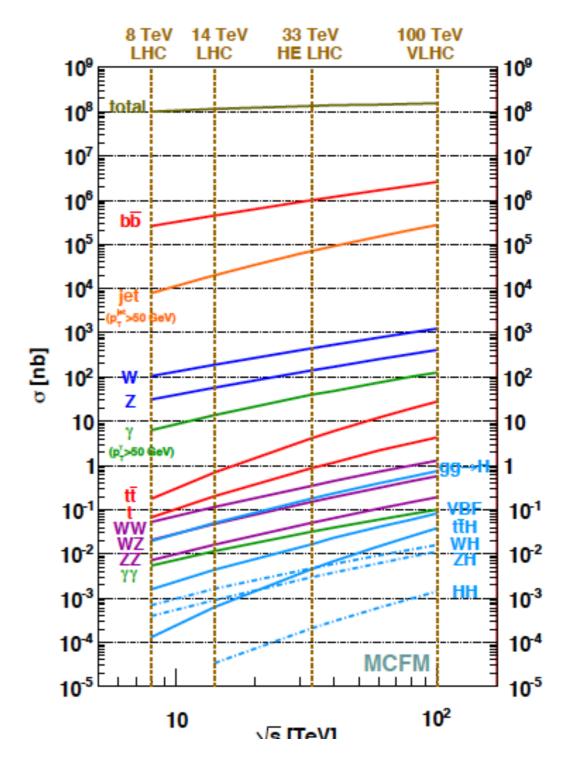
- ttW is one process that can lead to same-sign leptons, missing energy and b quarks.
- This signature is common in BSM searches.
- Currently same sign di-lepton analyses must rely on theory to assess backgrounds.
- Other SM backgrounds, W[±]Z, $ZZ,W^{\pm}W^{\pm},WWW,W^{+}W^{-}Z.$ ZZZ, ttZ



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MCFM-Looking to the future

- Open MP version v7.0
- Release of MPI version.
- Working on first inclusion of NNLO for simple DY type processes — with a view to introducing more complicated processes.



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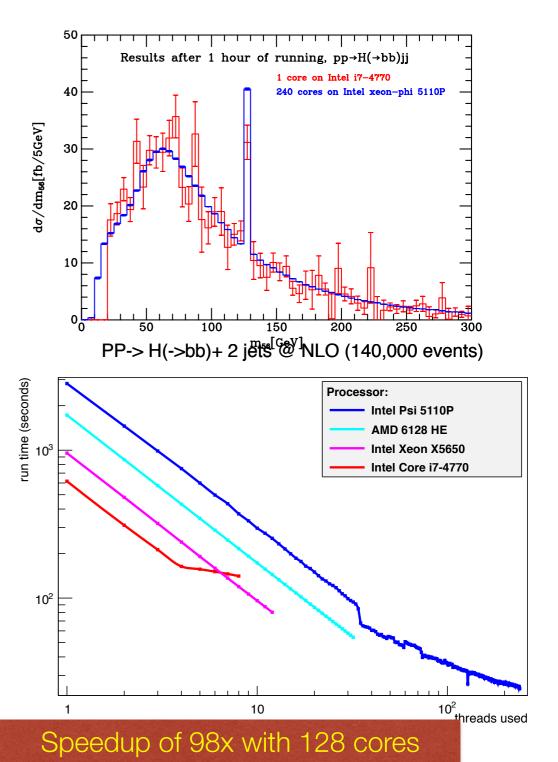
MCFM and Open Multi-processing

- * By putting, say, two cores in parallel, C→2C, f→f/2, V→V/2 at constant performance.
- Continued validity of Moore's law thus requires innovation in software, to deal with multi-threading in hardware.
 Keith FII

Keith Ellis, W&C, 8/21/2015

MCFM and Open Multi-processing

- OpenMP offers standardized way of exploiting multithreading.
- e.g. standard option for gfortran and intel compilers.
- Non destructive of the single thread code, (compiler directives interpreted as comments without openMP flag).
- Full statistics contributes to the adaptation of the VEGAS grid



Keith Ellis, W&C, 8/21/2015

One loop diagrams: NLO revolution

NLO pre-revolutionary techniques

- The classical paradigm for the calculation of one-loop diagrams was established in 1979.
- Complete calculation of one-loop scalar integrals.
- Reduction of tensor integrals to scalar integrals.

$$\int d^n l \frac{l^\mu}{(l^2 - m_1^2 + i\varepsilon)((l+p)^2 - m_2^2 + i\varepsilon)}$$

Nuclear Physics B153 (1979) 365-401 © North-Holland Publishing Company

SCALAR ONE-LOOP INTEGRALS

G. 't HOOFT and M. VELTMAN

Institute for Theoretical Physics*, University of Utrecht, Netherlands

Received 16 January 1979

Nuclear Physics B160 (1979) 151-207

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ONE-LOOP CORRECTIONS FOR e^+e^- ANNIHILATION INTO $\mu^+\mu^-$ IN THE WEINBERG MODEL

G. PASSARINO* and M. VELTMAN

Institute for Theoretical Physics, University of Utrecht, Utrecht, The Netherlands

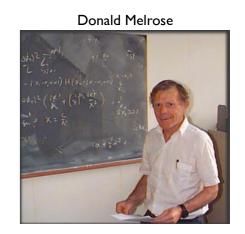
Received 22 March 1979

NLO revolution: Basis set of scalar integrals

 Any one-loop amplitude, with no matter how many legs, can be written as a linear sum of box, triangle, bubble and tadpole integrals

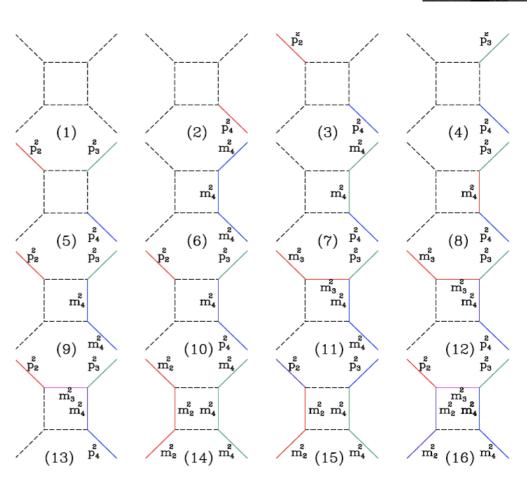
$$\mathcal{A}_N(\{p_i\}) = \sum d_{ijk} + \sum c_{ij} + \sum b_i$$

- In the context of NLO calculations scalar higher point functions can be expressed as a sum of box integrals.
- This result present in the 1965 thesis of Donald Melrose.
- In short, if we know the box, triangle, bubble and tadpole integrals, and their coefficients, we know everything.



QCDLoop: Basis set of 16 divergent box integrals

- 't Hooft and Veltman's integrals contain internal masses, however in QCD many lines are approximately massless.
- The consequent soft and collinear divergences are regulated by dimensional regularization.
- Invention of algorithm that defines the basis set for box integrals.
- Analytic and numerical results for 16 divergent box integrals.
- QCDLoop completely solves the problem of one loop integrals.
- http://qcdloop.fnal.gov



RKE, Zanderighi 0712.1851

Dashed lines are massless, line of the same color have same virtuality and/or mass

Other revolutionaries: Unitarity for I-loop diagrams

Techniques for determining the coefficients of the loop integrals

- Important steps include:-
- First modern use of the idea Bern, Dixon, Kosower
- Cuts w.r.t. loop momenta to give box coefficients directly Britto, Cachazo and Feng
- OPP reduction scheme Ossola, Papadopoulos, Pittau
- Combining the OPP procedure with unitarity RKE, Giele, Kunszt
- D-dimensional unitarity. Giele, Kunszt, Melnikov

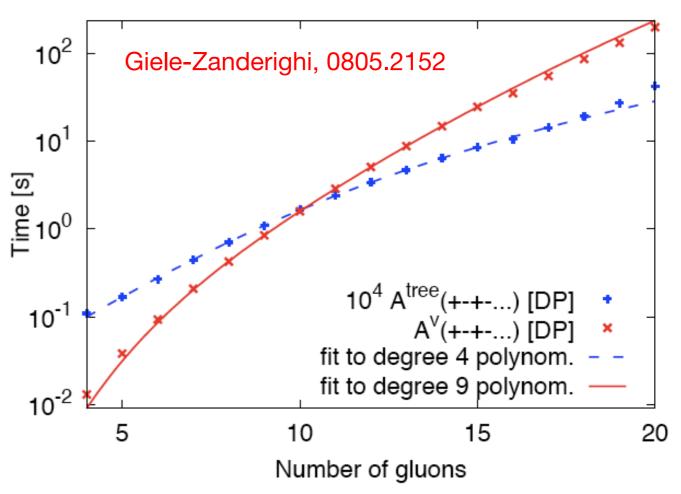
One-loop calculations of pure gluon amplitudes

- Time to calculate one-loop amplitude scales as N⁹ as expected. For small numbers of legs, N=4,5,6 the times are of the order of milliseconds.
- d-dimensional unitarity is a disruptive technology.
- Semi-numerical methods are the basis of most automatic procedures for determining oneloop amplitudes.

4g: RKE, Sexton 1985

5g: Bern, Dixon, Kosower, 1993

6g: RKE, Zanderighi, 2006



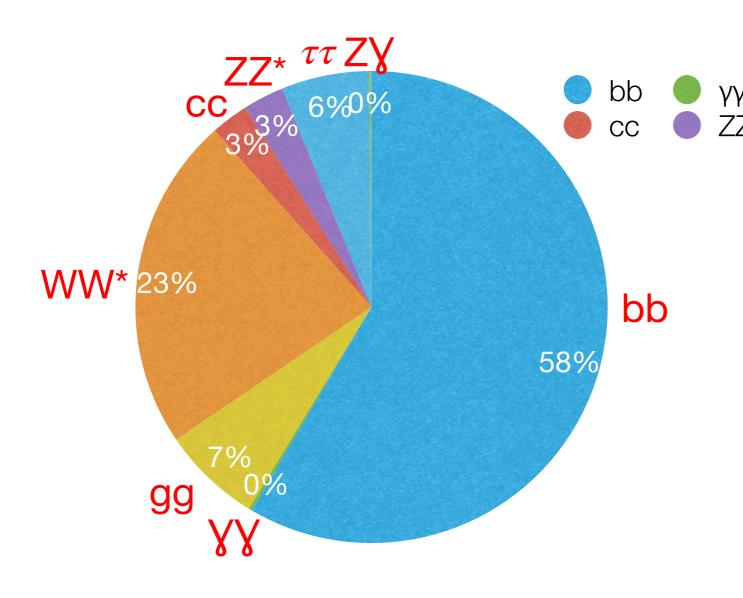


Subsequent automatic NLO programs

- Fully automatic procedures.
 - Madgraph5_aMC@NLO 1405.0301
 - Helac-I Loop 1502.01521
 - Go-Sam 1404.7096
- Approaches for greater number of legs of a less automatic nature.
 - Blackhat-Sherpa 1310.2808
 - Njet 1312.7140

The Higgs boson and interference

How can we probe a 4 MeV width for the Higgs?



Particle	Width[MeV]	Lifetime[s]
t	$\sim 1,300$	$\sim 5 \times 10^{-25}$
W	$\sim 2,000$	$\sim 3 \times 10^{-25}$
Z	$\sim 2,500$	$\sim 2.6 \times 10^{-25}$
h	4.21 ± 0.16	$\sim 1.65 \times 10^{-22}$
b	4.4×10^{-10}	$\sim 1.5 \times 10^{-12}$

 Large number of observable SM Higgs decays

 WW^*

Zgam

gg

- We will consider ZZ*,WW*.
- ZZ* branching ratio is 3%, (but before BR to observable mode).
- Γ_HSM ≈ 4 MeV, c.f. jet resolution ~ I GeV.

Keith Ellis, W&C, 8/21/2015

Rescaling properties of the cross section on the peak

• In the narrow width approximation

$$\sigma(i \to H) \times BR(H \to X) = |M(i \to h)|^2 \frac{\Gamma(h \to X)}{\Gamma_h} \sim \frac{g_i^2 g_f^2}{\Gamma_h}$$

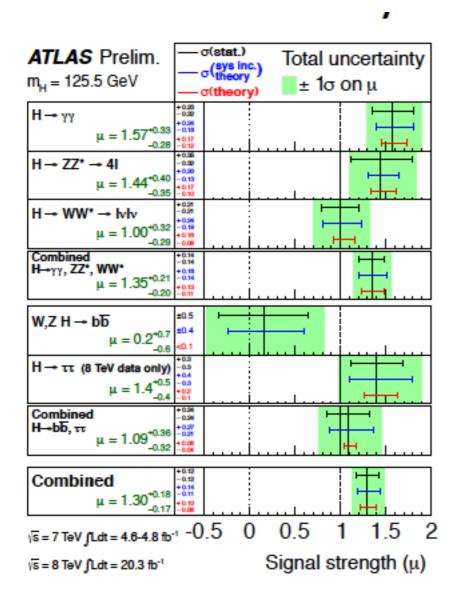
- Measurements on the Higgs peak, are only sensitive to the ratio, $g_i^2 g_f^2$
- Performing the rescaling by κ leaves the on-shell rate unchanged.

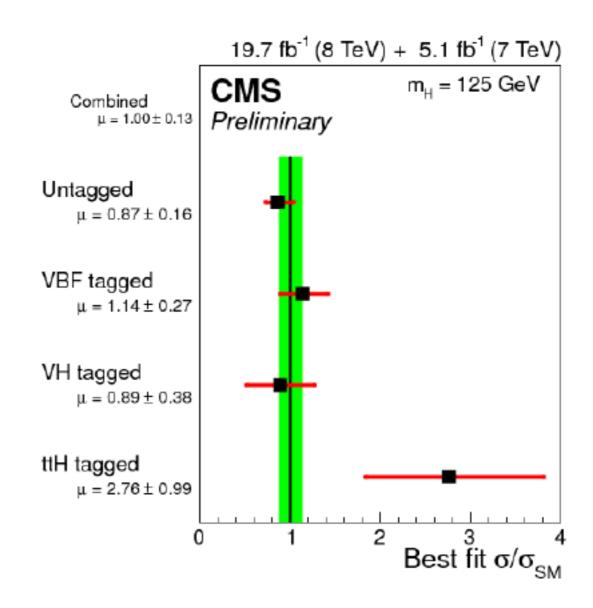
$$g_i \to \kappa g_i$$

$$g_f \to \kappa g_f$$

$$\Gamma_H \to \kappa^4 \Gamma_H$$

Signal strength measurements





• Signal strength measurements, (that assume a value for the total width), confirm that $g_i^2 g_f^2 / \Gamma_h$ is close to its standard model value (with ~20% errors)

Keith Ellis, W&C, 8/21/2015

Narrow width approximation for Higgs production

$$\frac{1}{(\hat{s} - M_h^2)^2 + M_h^2 \Gamma_h^2} \approx \frac{\pi}{M_h \Gamma_h} \, \delta(\hat{s} - M_h^2) \; .$$

• For the standard model Higgs, $\Gamma/M_h = 1/30,000$ so narrow width approximation should apply.....

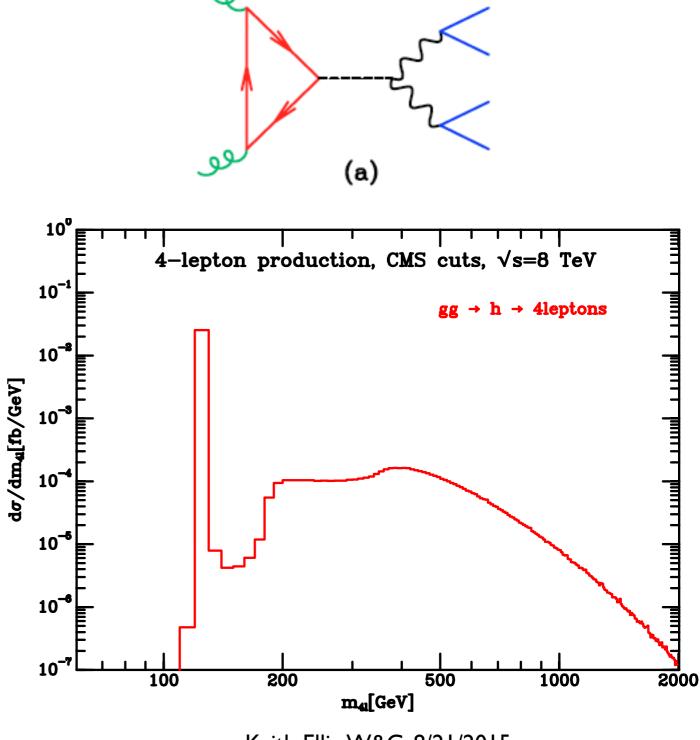
Narrow width approximation for Higgs boson

- How can it fail?
 - $\Gamma_H / M_H = 1/30,000$

• It fails spectacularly for $gg \rightarrow H \rightarrow ZZ^{(*)} \rightarrow e^-e^+\mu^-\mu^+$.

Kauer, Passarino, arXiv:1206.4803

 At least 10% of the cross section comes from m_{4l}>130GeV.



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Interference in pp \rightarrow ZZ \rightarrow e $^-$ e $^+$ $\mu^ \mu^+$

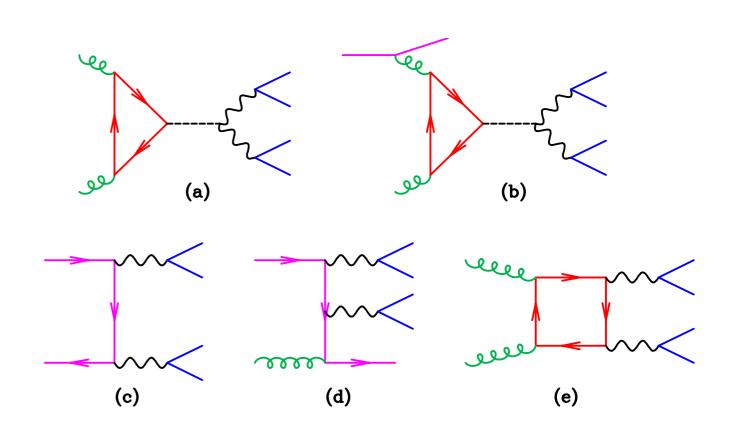
$$p + p \to H \to ZZ$$

$$\downarrow \qquad \qquad \downarrow \qquad \qquad \qquad \downarrow \qquad \qquad \qquad \qquad \downarrow \qquad \qquad \qquad \downarrow \qquad \qquad \qquad \downarrow \qquad \qquad \qquad \downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow \qquad \qquad$$

- We cannot consider the Higgs process alone.
- Both interfering and non-interfering backgrounds.

$pp \rightarrow e^-e^+\mu^-\mu^+$ in the standard model

- Mishmash of orders in perturbation their
- Representative diagrams are:-
- (a) and (e), (b) and (d)can interfere.
- (b-d) interference does not overwhelm (a-e)

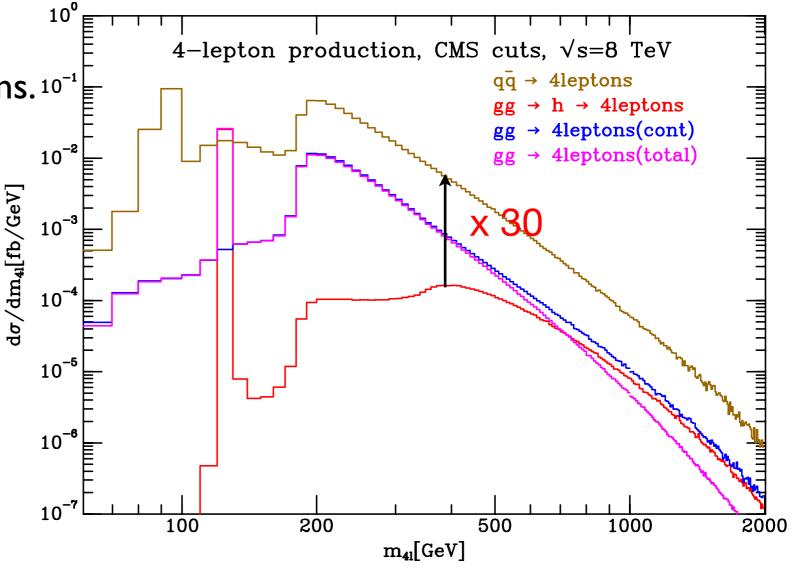


The big picture @ 8TeV

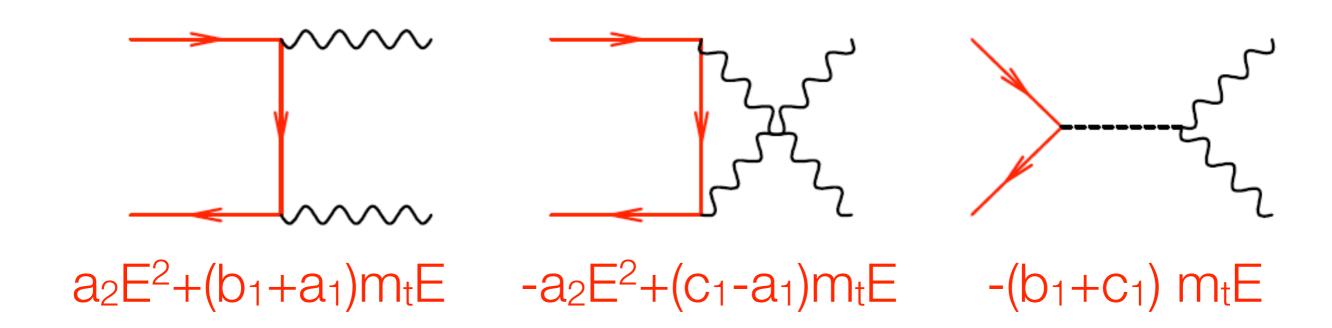
 $p_{T,\mu} > 5 \text{ GeV}, \ |\eta_{\mu}| < 2.4,$ $p_{T,e} > 7 \text{ GeV}, \ |\eta_{e}| < 2.5,$ $m_{ll} > 4 \text{ GeV}, \ m_{4\ell} > 100 \text{ GeV}$

CMS cuts CMS PAS HIG-13-002

- Peak at Z mass due to singly resonant diagrams. 10⁻¹
- Interference is an important effect offresonance.
- Destructive at large mass, as expected.
- With the standard model width, \(\Gamma_H\), challenging to see enhancement/deficit due to Higgs channel.

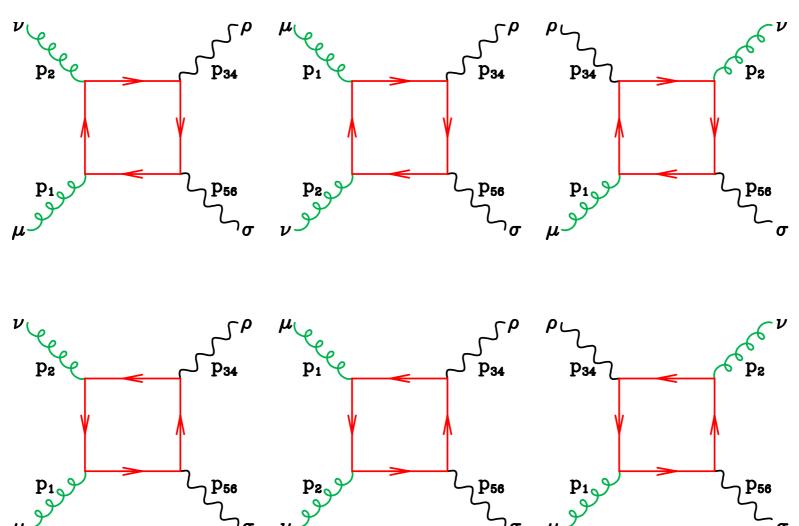


Higgs being Higgs



- First cancellation due to the gauge structure
- Second cancellation requires the Higgs
- c.f Lee, Quigg and Thacker

Diagrams for $gg \rightarrow Z/g^* + Z/g^*$ (background)



- We perform a stable, analytic calculation of these diagrams and their interference with the Higgs diagrams.
- Obtaining numerical stability is challenging for automatic procedures. Human intervention required.

Caola-Melnikov method for Higgs width

 Higgs cross section under the peak, section depends on ratio of couplings and width.

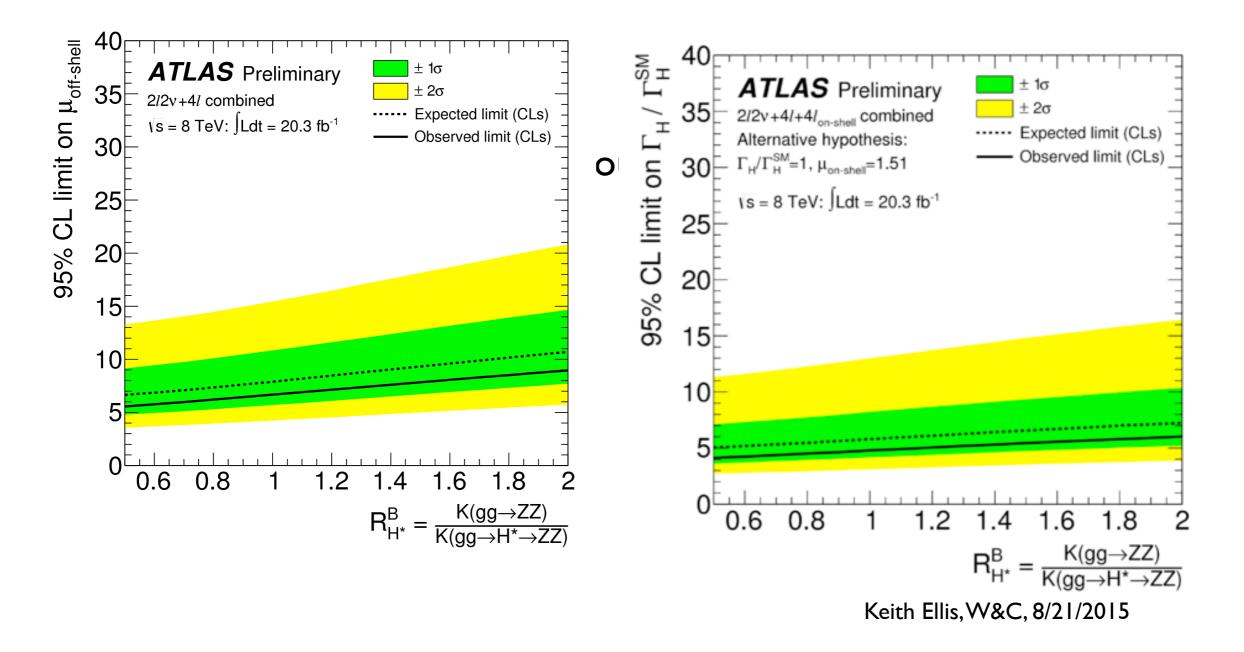
$$\sigma_{
m peak} \propto rac{g_i^2 g_f^2}{\Gamma}$$

- Measurements at the peak cannot untangle couplings and width.
- ullet Off-peak cross section is independent of the width, but still depends on $g_i^2g_f^2$ (modulo interference, see later). $\sigma_{
 m off}\propto g_i^2g_f^2$

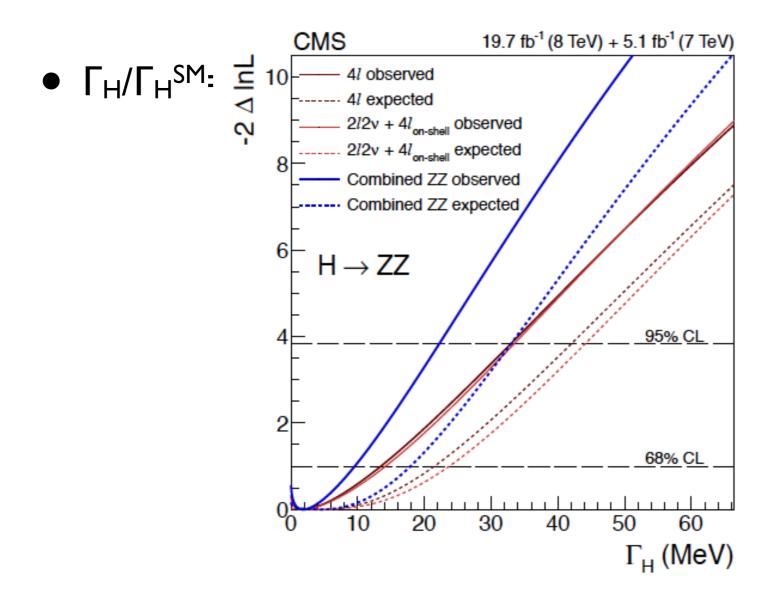
$$\frac{\left(\frac{\sigma_{\text{off}}}{\sigma_{\text{peak}}}\right)_{\text{experimental gg}}}{\left(\frac{\sigma_{\text{off}}}{\sigma_{\text{peak}}}\right)_{\text{theoretical SM}}} = \frac{\Gamma}{\Gamma^{\text{SM}}}$$

ATLAS result

 Presented as a function of the unknown relative K factor between "signal" and "background".



CMS result



Model-dependence of Higgs width bound.

- The bound on the Higgs width holds under the assumption that the coupling constants remain the same over a large span of energy $\sqrt{s=126} \rightarrow \sim 500$ GeV.
- $\mu_{ZZ}^{\text{on}} \equiv \frac{\sigma_h \times \text{BR}(h \to ZZ \to 4\ell)}{[\sigma_h \times \text{BR}(h \to ZZ \to 4\ell)]_{\text{SM}}} \sim \frac{\kappa_{ggh}^2 \kappa_{hZZ}^2}{\Gamma_h/\Gamma_h^{\text{SM}}},$ $\mu_{ZZ}^{\text{off}} \equiv \frac{d\overline{\sigma}_h}{[d\overline{\sigma}_h]_{\text{SM}}} \sim \kappa_{ggh}^2(\hat{s}) \kappa_{hZZ}^2(\hat{s}),$
- If new phenomena are present, this will not always be true.

Englert and Spannowsky, 1405.0285

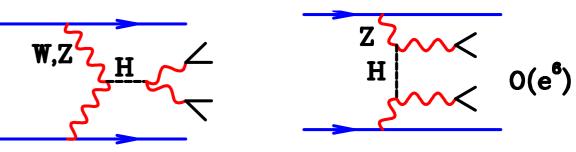
- In all cases there is great interest in the measurement of the gluon induced 4-lepton cross section away from the Higgs peak.
- If there is a large scale separation between the new phenomena and the off-shellness probed, this can be treated using an effective operator formulation.

Cacciapaglia et al, 1406.1757 Azatov et al, 1406.6338 Gaines et al, 1403.4951

Theoretical predictions for Vector Boson Fusion

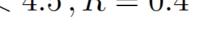
Diagrams for pp \rightarrow jet+jet+e⁻e⁺ μ - μ ⁺

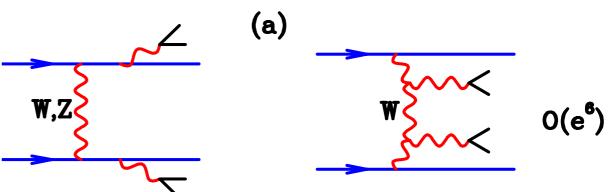
 Off-shell behaviour for VBF subject of much theoretical study.



Jet cuts

$$p_{T,J} > 30 \text{ GeV}, |\eta_J| < 4.5, R = 0.4$$





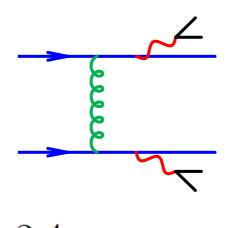
(b)

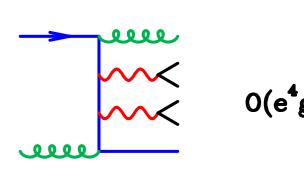
(c)

CMS lepton cuts

$$p_{T,\mu} > 5 \text{ GeV}, |\eta_{\mu}| < 2.4,$$

 $p_{T,e} > 7 \text{ GeV}, |\eta_{e}| < 2.5,$
 $m_{ll} > 4 \text{ GeV}, m_{4\ell} > 100 \text{ GeV}.$





Additional VBF cuts

$$y_{gap} > 2.4$$

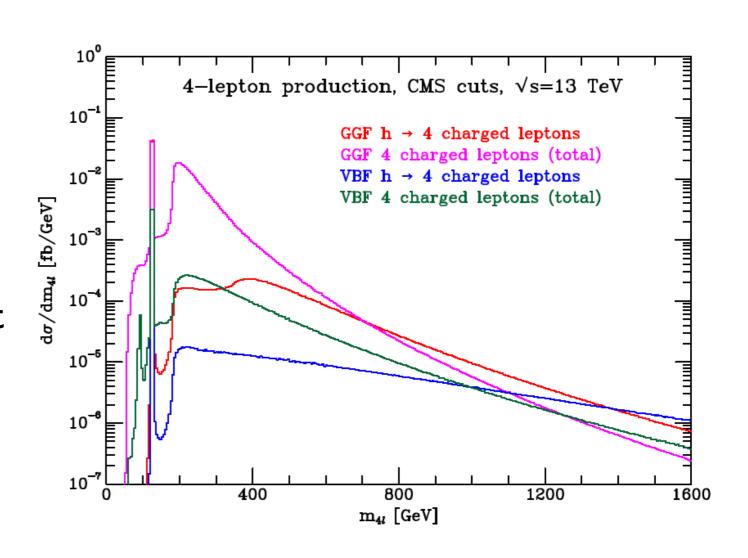
$$\eta_1 \times \eta_2 < 0$$

$$m_{j_1 j_2} > 500 \text{ GeV}$$

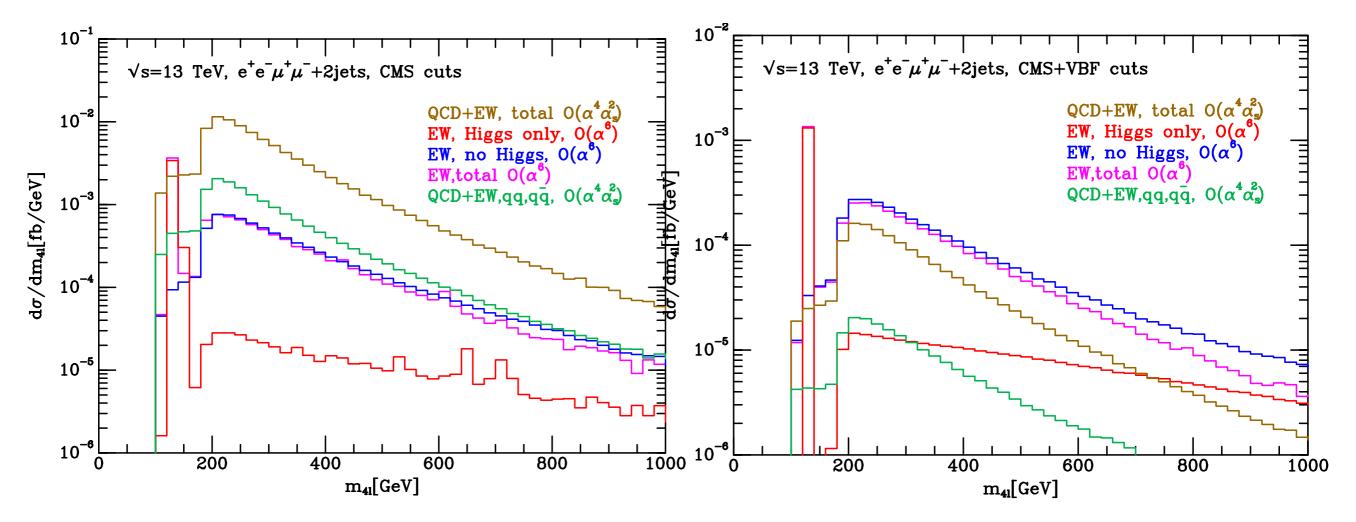
Gluon-gluon fusion vs Vector boson fusion

• (pp \rightarrow e⁻e⁺ μ - μ ⁺) vs (pp \rightarrow jet+jet+e⁻e⁺ μ - μ ⁺ with VBF cuts)

- EW cross section for Higgs ~10% of gg fusion (before VBF cuts)
- Higgs tail relatively more important in pp → jet+jet +e⁻e⁺µ⁻µ⁺
- Different slope for VBF tail.

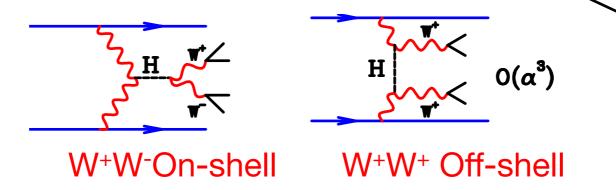


VBF cuts @ 13 TeV



- Run II will give us access to VBF
- VBF cuts reduce the strong background, $O(\alpha^4 \alpha_s^2)$, but gq -> gq e⁻e⁺ μ - μ ⁺ still significant.
- This same statement holds for W+W-,W±Z,ZZ

Most useful channel is W+W- vs W+W+



- In the first instance, we work in the effective coupling framework, where standard couplings are rescaled by κ_{\lor} .
- At \sqrt{s} =8TeV, SM prediction displays a dependence on κ_V

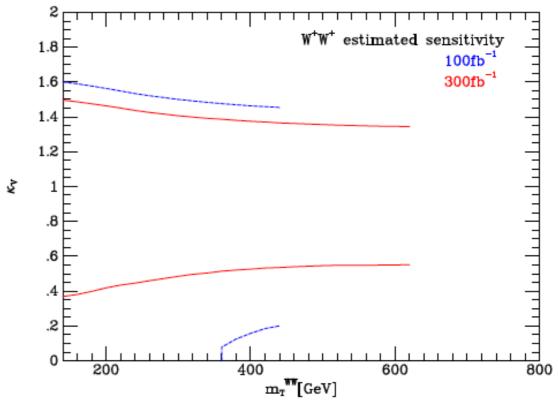
$$\sigma_{fiducial}^{same-sign} = 1.015 - 0.106 \, \kappa_V^2 + 0.040 \, \kappa_V^4 \; \text{fb}$$
 .

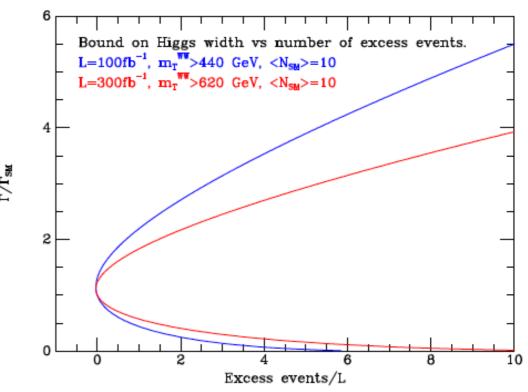
- ATLAS on-shell signal-strength $\mu_{VBF}^{ATLAS} = 1.27^{+0.53}_{-0.45}$
- ATLAS W⁺W⁺ measurement $\sigma^{measured} = 1.3 \pm 0.4(stat) \pm 0.2(syst)$ fb.
- Bound is $\kappa V < 7.8$.
- ullet current notional width bound $\Gamma_H < 60.8 imes \Gamma_H^{SM}$.

New idea

Improvement with 100, 300fb⁻¹ at \sqrt{s} =13TeV

- Expected upper and lower bounds on Ky obtained from W+W+ events as a function of the transverse mass.
- Bounds are cut off when SM prediction falls below 10 events.
- In all cases the best bounds are achieved, taking the highest possible cut on the transverse mass.
- Possible width bounds with (100, 300fb⁻¹) are similar to those currently obtained from gg fusion (20fb⁻¹).





Effective coupling dependence of other processes

- $\sqrt{s}=13\text{TeV} \text{ in } 100\text{fb}^{-1}$
- M_(T)>300GeV
- Note that numbers are not so different for $\kappa_v=0$ (no Higgs) and $\kappa_V=1$ (SM)
- For this energy and luminosity we cannot place the cut sufficiently high that the noncancelling terms dominate.

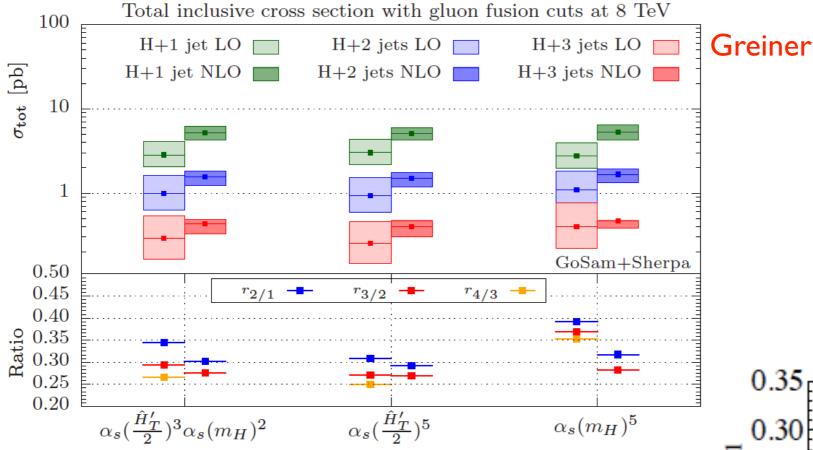
 $l^-l^+\nu\bar{\nu}: N^{\text{off}} = 127.9 - 42.8\,\kappa_V^2 + 20.8\,\kappa_V^4$ $l^{+}l^{+}\nu\nu: \qquad N^{\text{off}} = 37.2 - 18.3 \,\kappa_{V}^{2} + 8.3 \,\kappa_{V}^{4}$ $l^{-}l^{-}\bar{\nu}\bar{\nu}: \qquad N^{\text{off}} = 11.0 - 4.1 \,\kappa_{V}^{2} + 1.8 \,\kappa_{V}^{4}$ $l^{+}l^{-}l^{+}\nu: \qquad N^{\text{off}} = 23.5 - 6.8 \,\kappa_{V}^{2} + 3.2 \,\kappa_{V}^{4}$ $l^{+}l^{-}l^{-}\bar{\nu}: \qquad N^{\text{off}} = 11.3 - 3.3 \,\kappa_{V}^{2} + 1.6 \,\kappa_{V}^{4}$ $l^-l^+l^-l^+: N^{\text{off}} = 6.0 - 3.0 \,\kappa_V^2 + 1.5 \,\kappa_V^4$

 $l^-l^+\nu\bar{\nu}: N^{\text{off}} = 224.8 - 42.8 \,\kappa_V^2 + 20.8 \,\kappa_V^4$ $N^{\text{off}} = 9.0 - 3.0 \,\kappa_V^2 + 1.5 \,\kappa_V^4$

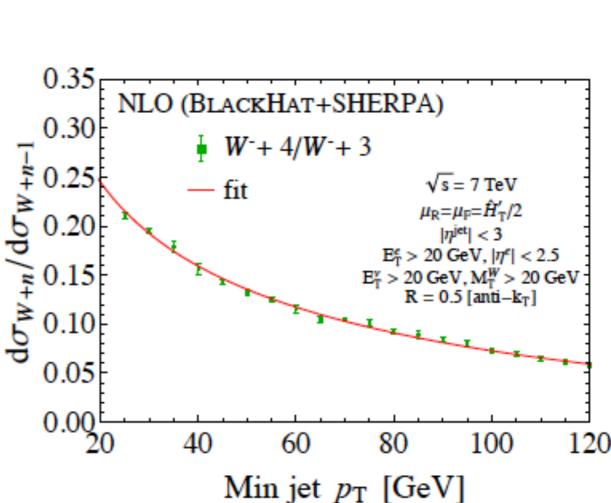
Perturbative QCD 2015 and onwards

- The most significant result of Run I of the LHC is the discovery of the Higgs boson in 2012
- Higgs boson (produced predominantly by gluon fusion) radiates copiously, thus emphasizing the importance of radiative corrections.
- e.g. for Higgs total cross section $\sigma = 12.937 \times (1 + 1.28 + 0.77)$.
- Perturbative QCD is front and centre in the physics program of run II.
- "With data taken in coming years at or near to the design energy of I4 TeV, a broader picture of physics at the TeV scale will emerge with implications for the future of the energy frontier program. Amongst the essential inputs will be precision measurements of the properties of the Higgs boson and direct searches for new physics that will make significant inroads into new territory." ATLAS Physics at High Luminosity, I 307.7292

Propensity to radiate



"Berends-Giele" ratio greater for Higgs than for W



The next frontier: NNLO

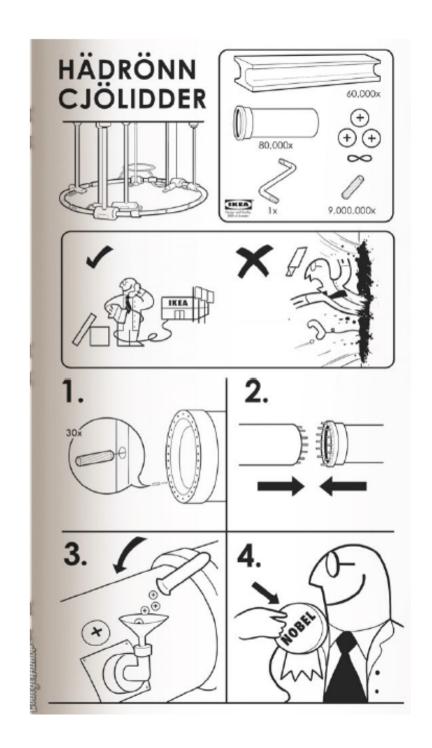
- NNLO calculations roughly at the level of NLO in 1990.
 - NLO 2 to 2 virtual matrix elements known
 - NLO top cross section (total and differential) known
 - NLO 2 to 3 calculations just beginning to be tackled?
- NLO calculations complete ~2010
- Will we make faster progress on NNLO?

NNLO - 2 loop matrix elements

- Tremendous advance in analytical methods
- differential equations, canonical basis of integrals,....
- $2\rightarrow 2$ processes with four independent scales seem to be within reach, but extension to $2\rightarrow 3$ processes, eg gg $\rightarrow V_1V_2$ g seem currently out of reach.
- If $2\rightarrow 3$ represents a wall, then we need to investigate other methods.
- The investment in numerical methods compared to analytic methods, seems to me to be too small.
 - Contour deformation in FP space, sector decomposition Schlenk
 - Contour deformation in momentum space, e.g. Becker, Weinzierl 1211.0509

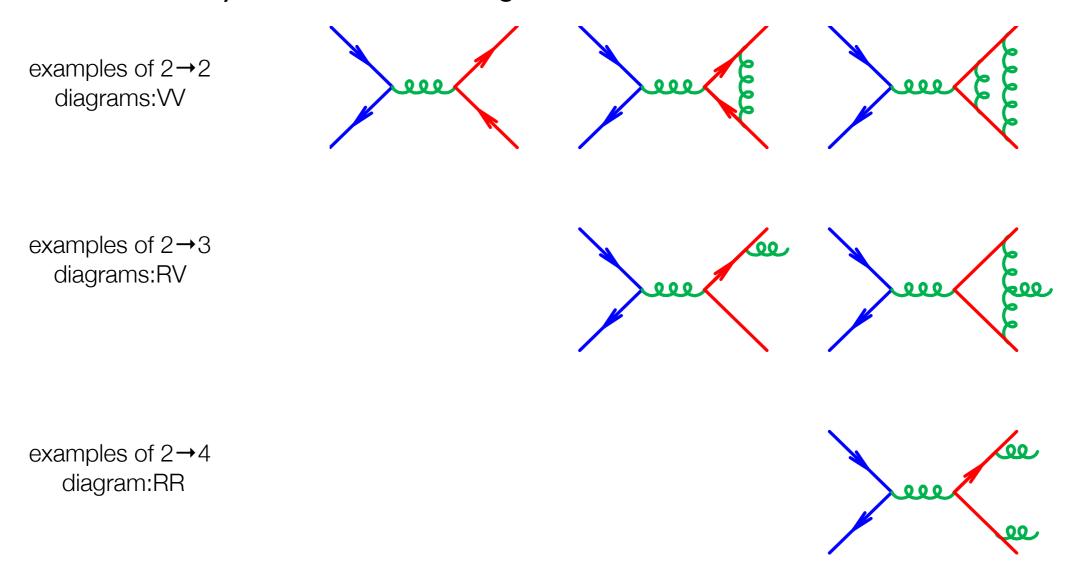
NNLO-some assembly required

- Contributions from Real-Real, Real-Virtual and Virtual-Virtual.
- For the lower multiplicities the poles are explicit, whereas as for higher multiplicities, they appear after integration.
- Thus the requirement to cancel the poles appears to be in contradiction with the desire for a differential cross section.



NNLO diagrams

• Challenge is not the calculation of the individual diagrams, but rather the assembly of pieces that individually contain infrared divergences



• In different regions of phase space, different subsets of partons lead to singularities of the matrix elements.

NNLO - Four main combination methods

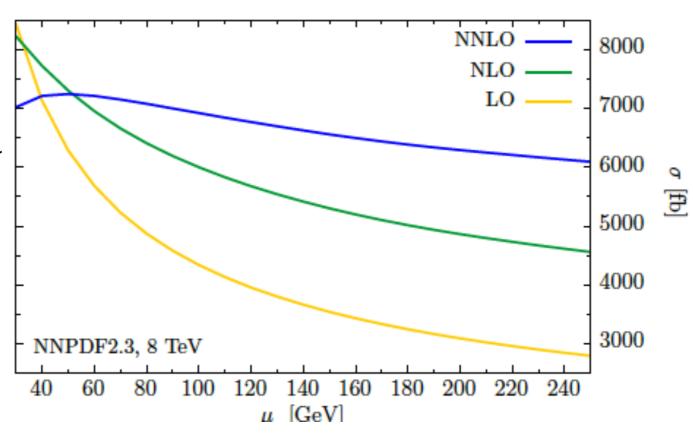
Antenna

- Pros:Analytic cancellation of poles, demonstrated for 2->2 colored scattering
- Con: More challenging interface to existing NLO codes
- Sector improved residue subtraction scheme.
 - Pros:Brute force method, offers possibility of generalization to arbitrary processes, demonstrated for 2->2 colored scattering
 - Con: Numerical cancellation of poles
- qt/N-jettiness subtraction
 - Pro:Meshes well with existing NLO codes
 - Con:Slicing method, have to demonstrate independence from cutoff parameter.
- Colour subtraction
 - Pro:Local subtraction terms
 - Con: No NNLO application to processes with initial state hadrons yet.

Boughezal et al, 1504.07922, 1505.03893 Caola et al, 1508.02684

Higgs+I jet

- σ =17.5+1.1-1.4pb
- QCD corrections depend on the kinematics, (K-factor dependent on p_T cut)
- Also results for pure glue from Chen et al, 1408.5325
- We look forward to a detailed comparison of the two (three) results



At 13 TeV in effective theory

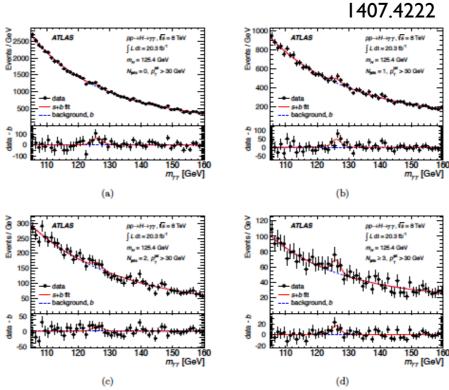
Process	α_s^2	α_s^3	α_s^4	α_s^5
$\sigma(pp \to H) \text{ pb [1]}$	13	30	40	43
$\sigma(pp \to H + \text{jet}) \text{ pb[2]}$		10	15	18
$\sigma(pp \to H+ 2 \text{ jet}) \text{ pb[3]}$			3.5	5.1
$\sigma(pp \to H + 3 \text{ jet}) \text{ pb[3]}$				1.6

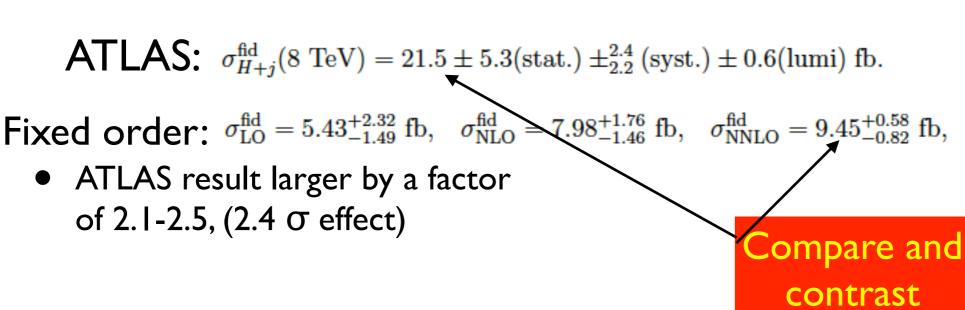
+ $O(\alpha^6_s)$ results

from Greiner here

Higgs + I jet, (fiducial cross section)

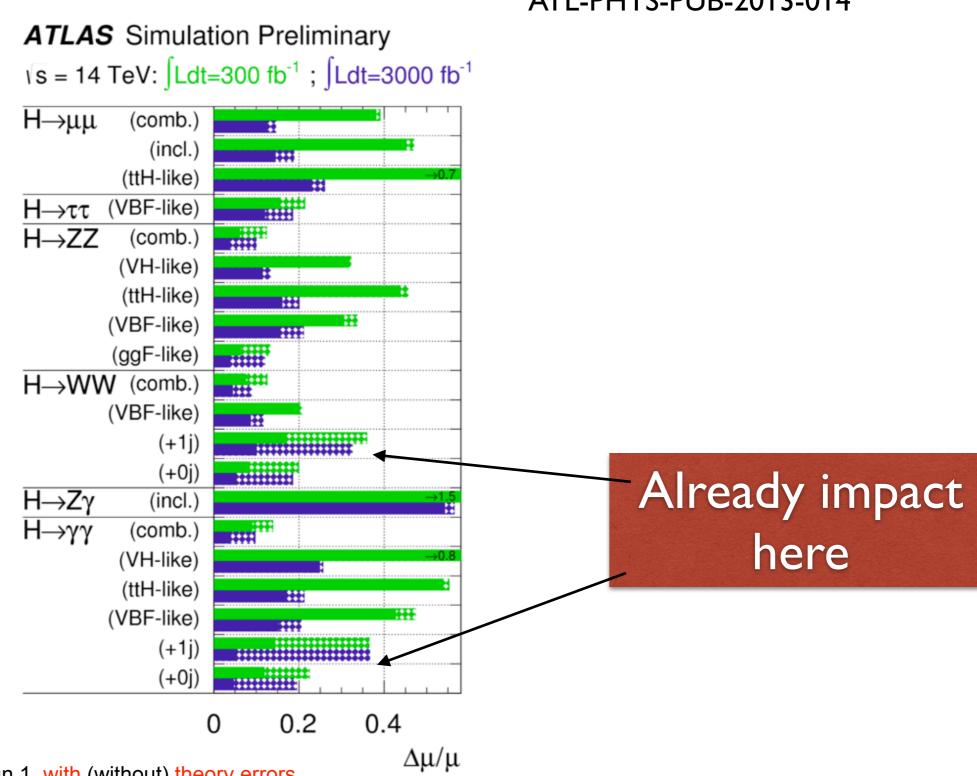
- ATLAS has published Higgs cross section separated by the number of jets, in their fiducial region.
- Allow comparison of their results with new NNLO results (Caola et al, 1508.02684) in their fiducial region.





Influence of theory on signal strengths





ATLAS: Syst. errors as run 1, with (without) theory errors

NNLO: Wish-listeria I

A judicious combination of the desirable and the possible?

Process	State of the Art	Desired	Delivered
H d σ @ NNLO QCD (expansion in $1/m_t$		$d\sigma$ @ NNNLO QCD (infinite- m_t limit)	1503.06056[2]
	full m_t/m_b dependence @ NLO QCD	full $m_{\rm t}/m_{\rm b}$ dependence @ NNLO QCD	
	and @ NLO EW	and @ NNLO QCD+EW	
	NNLO+PS, in the $m_t \to \infty$ limit	NNLO+PS with finite top quark	
		mass effects	1309.0017[3], 1501.04637[4] 1407.3773[5]
H + j	$d\sigma$ @ NNLO QCD (g only)	$d\sigma$ @ NNLO QCD (infinite- $m_{\rm t}$ limit)	1408.5325[6],1504.07922[7],1505.03893[8]
	and finite-quark-mass effects	and finite-quark-mass effects	
	@ LO QCD and LO EW	@ NLO QCD and NLO EW	
H + 2j	$\sigma_{\text{tot}}(\text{VBF})$ @ NNLO(DIS) QCD	$\mathrm{d}\sigma(\mathrm{VBF})$ @ NNLO QCD + NLO EW	1506.02660[9]
	$d\sigma(VBF)$ @ NLO EW		
	$d\sigma(gg)$ @ NLO QCD (infinite- m_t limit)	$d\sigma(gg)$ @ NNLO QCD (infinite- m_t limit)	
	and finite-quark-mass effects @ LO QCD	and finite-quark-mass effects	
		@ NLO QCD and NLO EW	
H + V	dσ @ NNLO QCD	with $H \to b\bar{b}$ @ same accuracy	1501.07226[10]
	$d\sigma$ @ NLO EW	$d\sigma(gg)$ @ NLO QCD	
	$\sigma_{\rm tot}(\rm gg)$ @ NLO QCD (infinite- $m_{\rm t}$ limit)	with full $m_{\rm t}/m_{\rm b}$ dependence	
tH and	$d\sigma(\text{stable top})$ @ LO QCD	$d\sigma$ (top decays)	
ŧΗ		@ NLO QCD and NLO EW	
ttH	$d\sigma(\text{stable tops})$ @ NLO QCD	$d\sigma(\text{top decays})$	1407.0823[11]
		@ NLO QCD and NLO EW	
$gg \to HH$	$d\sigma$ @ NLO QCD (leading $m_{\rm t}$ dependence)	dσ @ NLO QCD	1408.2422[12, 13]
	$d\sigma$ @ NNLO QCD (infinite- $m_{\rm t}$ limit)	with full $m_{\rm t}/m_{\rm b}$ dependence	

Wish-listeria II

Process	State of the Art	Desired	Delivered
tt	$\sigma_{\rm tot}({\rm stable\ tops})$ @ NNLO QCD	$d\sigma(\text{top decays})$	1411.3007[15]
	$d\sigma(\text{top decays})$ @ NLO QCD	@ NNLO QCD $+$ NLO EW	
	$d\sigma$ (stable tops) @ NLO EW		
$t\bar{t} + j(j)$	$d\sigma$ (NWA top decays) @ NLO QCD	$d\sigma$ (NWA top decays)	
		@ NNLO QCD $+$ NLO EW	
$t\bar{t} + Z$	$d\sigma$ (stable tops) @ NLO QCD	$d\sigma$ (top decays) @ NLO QCD	
		+ NLO EW	
single-top	$d\sigma$ (NWA top decays) @ NLO QCD	$d\sigma$ (NWA top decays)	1404.7116[16]
		@ NNLO QCD $+$ NLO EW	
dijet	$d\sigma$ @ NNLO QCD (g only)	$d\sigma$ @ NNLO QCD + NLO EW	1412.3427[17], 15xx.xxxx
	$d\sigma$ @ NLO EW (weak)		
3j	$d\sigma$ @ NLO QCD	${ m d}\sigma$ @ NNLO QCD + NLO EW	
$\gamma + \mathbf{j}$	$d\sigma$ @ NLO QCD	${ m d}\sigma$ @ NNLO QCD + NLO EW	
	$d\sigma$ @ NLO EW		

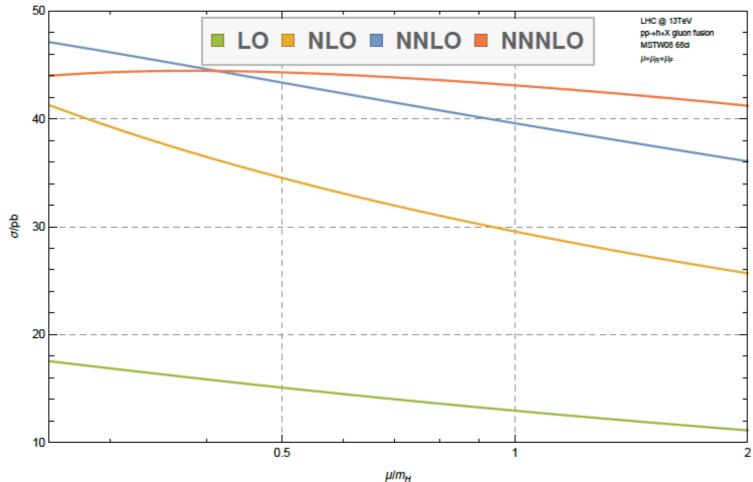
Wish-listeria III

Process	State of the Art	Desired	Delivered
V	$d\sigma(lept. \ V \ decay)$ @ NNLO QCD	$d\sigma(lept. \ V \ decay)$ @ NNNLO QCD	
	$\mathrm{d}\sigma(\mathrm{lept.}\ \mathrm{V}\ \mathrm{decay})$ @ NLO EW	and @ NNLO QCD+EW	
		NNLO+PS	1407.2940[18]
V + j(j)	$d\sigma(lept. \ V \ decay)$ @ NLO QCD	$d\sigma(lept. \ V \ decay)$	
	$\mathrm{d}\sigma(\mathrm{lept.}\ \mathrm{V}\ \mathrm{decay})$ @ NLO EW	@ NNLO QCD $+$ NLO EW	1504.02131[10]
VV'	$d\sigma(V \text{ decays})$ @ NLO QCD	$d\sigma(\text{decaying off-shell V})$	1309.7000[19], 1405.2219[20],1408.5243[21], 1504.01330[22]
	$\mathrm{d}\sigma(\mathrm{on}\text{-shell V decays})$ @ NLO EW	@ NNLO QCD $+$ NLO EW	
$gg \to VV$	$d\sigma(V \text{ decays}) @ LO QCD$	$d\sigma(V \text{ decays})$ @ NLO QCD	
$V\gamma$	$d\sigma(V \text{ decay})$ @ NLO QCD	$d\sigma(V \text{ decay})$	
	$\mathrm{d}\sigma(\mathrm{PA,\ V\ decay})$ @ NLO EW	@ NNLO QCD $+$ NLO EW	
Vbb	$d\sigma(lept. \ V \ decay)$ @ NLO QCD	$d\sigma(lept. \ V \ decay)$ @ NNLO QCD	
	massive b	+ NLO EW, massless b	
$VV'\gamma$	$d\sigma(V \text{ decays})$ @ NLO QCD	$d\sigma(V \text{ decays})$	
		@ NLO QCD $+$ NLO EW	
VV'V"	$d\sigma(V \text{ decays})$ @ NLO QCD	$d\sigma(V \text{ decays})$	
		@ NLO QCD $+$ NLO EW	
VV' + j	$d\sigma(V \text{ decays})$ @ NLO QCD	$d\sigma(V \text{ decays})$	
		@ NLO QCD $+$ NLO EW	
VV' + jj	$d\sigma(V \text{ decays})$ @ NLO QCD	$d\sigma(V \text{ decays})$	
		@ NLO QCD $+$ NLO EW	
$\gamma\gamma$	$d\sigma$ @ NNLO QCD + NLO EW	q_T resummation at NNLL	
		matched to NNLO	1505.03162[23]

Considerable amount of red ink since mid 2014!

Beyond N²LO: Higgs total cross section at N³LO

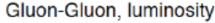


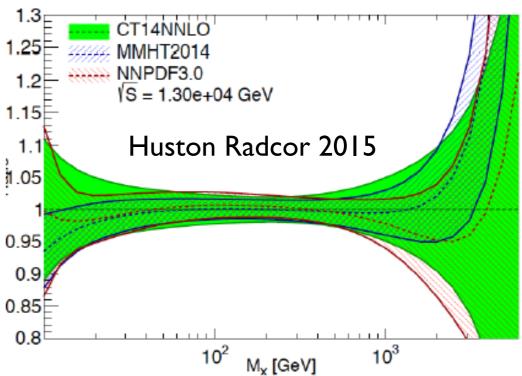


- σ = 44.31+0.31%-2.64%pb for $\mu \in [m_H/4, m_H]$ at N³LO
- At N²LO this uncertainty is ±9%

Uncertainty budget for gg->H

- According to Anastasiou et al, after the N^3LO calculation the dominant uncertainty is the PDF and α_s .
- However recent progress in PDF fits has reduced the uncertainty so that it is also at the 2% level.
- Most studies of the evolution of the uncertainty in the gluon distribution are targeted at larger x.





NNPDF down by 2-2.5%, CT14 up by \sim 1%, MMHT14 down by \sim 0.5%

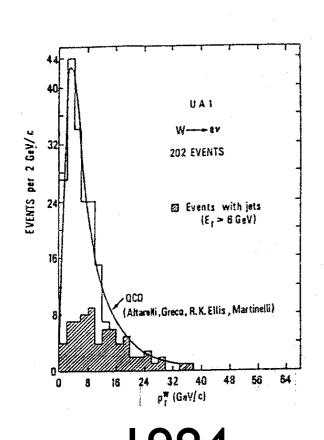
partially data, partially corrections in fitting code, partially changes in fitting procedures

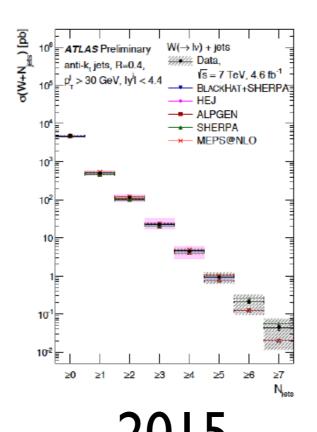
	CT14	MMHT2014	NNPDF3.0
scale = m _H			
8 TeV	18.66 pb -2.2% +2.0%	18.65 pb -1.9% +1.4%	18.77 pb -1.8% +1.8%
13 TeV	42.68 pb -2.4% +2.0%	42.70 pb -1.8% +1.3%	42.97 pb -1.9% +1.9%

The PDF uncertainty using this new generation of PDFs will be similar in size to the NNNLO scale uncertainty and to the $\alpha_e(m_z)$ uncertainty.

Summary

- It is a great time to work on radiative corrections. Higgs is a central theme of run II at the LHC; it radiates copiously.
- Perturbative QCD can improve the interpretation of LHC experiments. Fermilab would do well to continue to invest in this field.

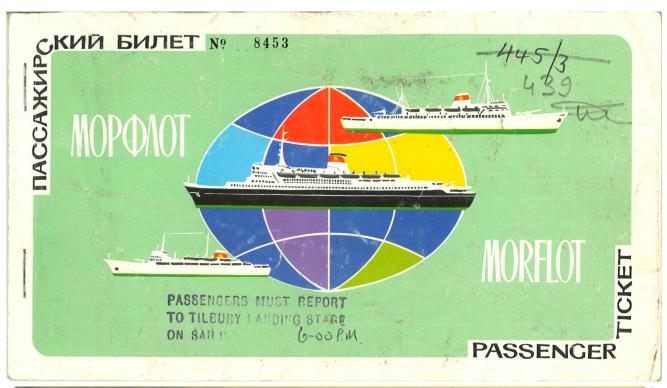




Keith Ellis, W&C, 8/21/2015

Historical remarks

- First visit to the US in 1977 on "Motorship Alexander Pushkin" — Fare ~\$200.
- Post-doc at MIT, (Radiative corrections to the DY process, K-factor)
- Post-doc at Caltech (ERT calculation allowing measurement of α_s in e+e-).
- Return to Europe in 1980.

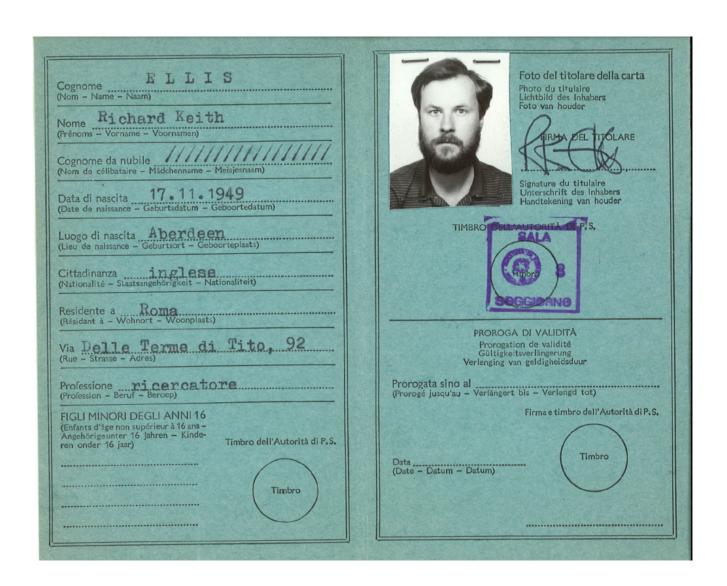


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Keith Ellis, W&C, 8/21/2015

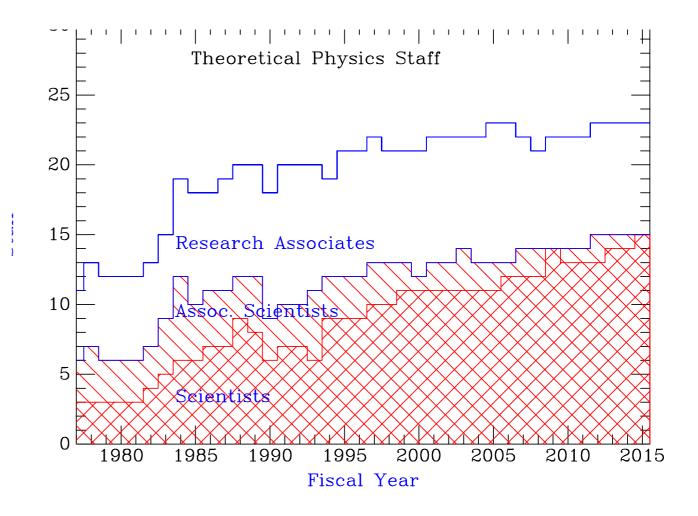
Return to USA

- Abandoned a semipermanent position in Rome to come to Fermilab
- Took up Associate Scientist appointment at Fermilab, on April 1st, 1984.



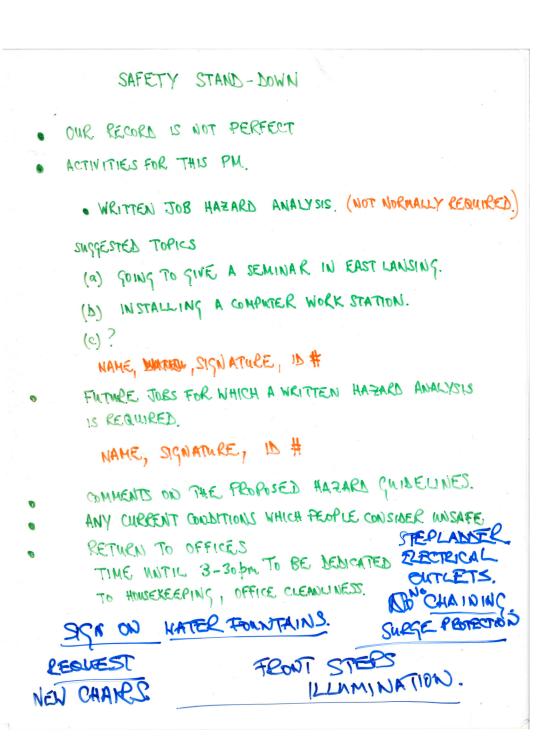
Theory Group

- In 1992 I was appointed by John Peoples as the head of the theory department.
- I served as head of the theory group from 1992 (when Bill Bardeen left for the SSC) until 2004, (with a sabbatical from 1995-1996).
- I had to handle all the standard stuff, travel, appointment of post-docs, promotions, reviews of the theory group (at that time, mercifully few and largely inconsequential).



Safety Stand-down

- In 1998 we had to deal with the "Safety Standdown"
- Safety is clearly an important issue.
- As group leader I had to conduct the safety standdown.
- It was a struggle to identify real hazards in theoretical physics department....



December 16, 1998 Theoretical Physics and Astrophysics Groups

Future Jobs for which written Job Hazard Analysis Required.

It is our considered opinion that as of today none of the jobs in the Theoretical Physics and Theoretical Astrophysics Depratments in the foreseeable future present sufficient risk to require a written Job Hazard Analysis. All signatories are aware that they are free to revoke this decision and bring potentially risky tasks to the attention of their supervisor should circumstances change in the future.

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KEITH ELLUS

Keith Ellis, W&C, 8/21/2015

Algebraic manipulation & Schoonschip





Schoonschip was
Veltman's algebraic
manipulation
program, which I ran
as a plugin to the
Atari-1040

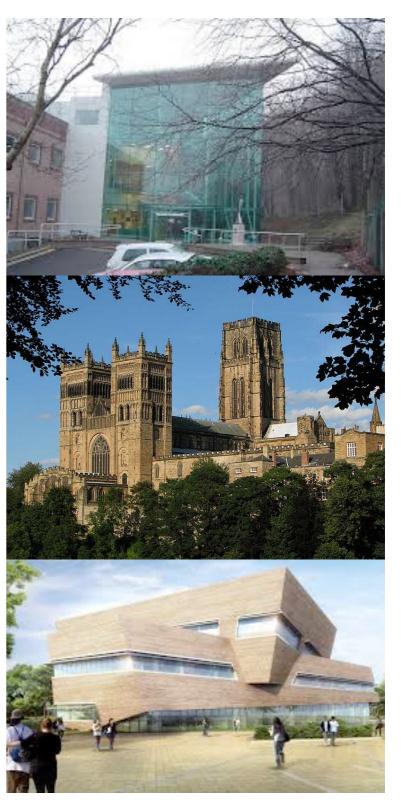




Science & Technology Facilities Council

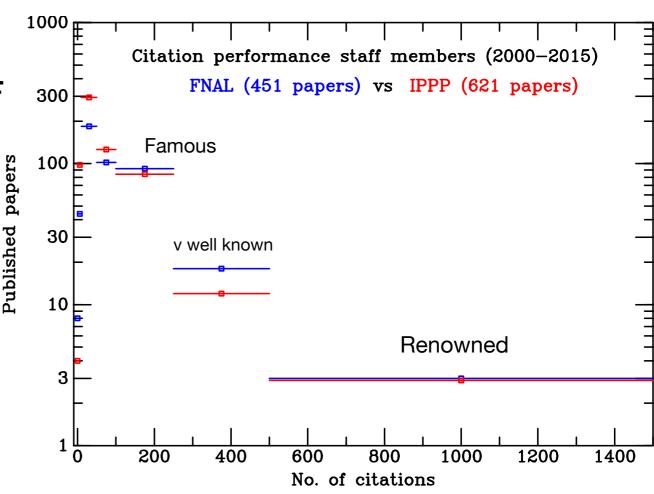
Transitions

- Director of Institute of Particle Physics Phenomenology (IPPP) in Durham from 10/1/2015
- Durham is a university and cathedral city, (a wee bit south of the Scottish border).
- 10/1/2015 —> 1/10/2015
- color —> colour
- renormalization —> renormalisation?
- 8 1/2" x 11" —> A4 (shorter and broader —> narrower and longer?)



IPPP: research record

- Some measure of the standing of the group can be obtained by the citation record, cf. the Fermilab theory group.
- Conclusion the two groups are roughly commensurate.
- I hope to continue a close working relationship with Fermilab.
- I hope that my colleagues in the theory department will continue to hire Durham students.





Aim 2: To develop high-quality international partnerships, networks and collaborations in all our areas of activity.

Thank you